

Q1) Solve using Cardon's method

$$x^3 - 15x^2 - 33x + 847 = 0 \quad \text{--- (1)}$$

solution: -

Removing the second term by diminishing the roots of the given equation

$$ax^3 + bx^2 + cx + d = 0$$

$$\Rightarrow h = -\frac{a_1}{na_0} = \frac{-(-15)}{3 \times 1} = 5$$

5	1	-15	-33	847
		5	-50	-415
	1	-10	-83	432
		5	-25	
	1	-5	-108	
		5		
	1	0		

Transformed equation is

$$y^3 - 108y + 432 = 0 \quad \text{--- (2)}$$

$$\text{Where } y = x - 5 \quad \text{--- (3)}$$

$$\text{Let } y = p^{1/3} + q^{1/3}$$

$$\Rightarrow y^3 = p + q + 3p^{1/3}q^{1/3}(p^{1/3} + q^{1/3})$$

$$\Rightarrow y^3 - 3p^{1/3}q^{1/3}y - (p+q) = 0 \quad \text{--- (4)}$$

Comparing (2) & (4)

$$p^{1/3}q^{1/3} = 36 \Rightarrow pq = 6^6$$

$$\& p + q = -432.$$

$\therefore p$  &  $q$  are the roots of

$$t^2 + 432t + (6)^6 = 0$$

$$\Rightarrow t^2 + 2(6)^3t + (6)^6 = 0$$

$$\Rightarrow (t + 6^3)^2 = 0$$

$$\Rightarrow t = -216, -216$$

$$\Rightarrow p = -216, q = -216$$

$$\Rightarrow p^{1/3} = -6, -6\omega, -6\omega^2$$

$$\& q^{1/3} = -6, -6\omega, -6\omega^2$$

$$x^2 - (x+y)t + t^2 - p = 0$$

$$q^{\sqrt[3]{3}} = -6, -6\omega, -6\omega^2$$

$$\begin{aligned} \therefore y &= p^{\sqrt[3]{3}} + q^{\sqrt[3]{3}} \\ &= (-6-6), (-6\omega-6\omega^2), (-6\omega^2-6\omega) \\ &= -12, 6, 6 \quad (\because 1+\omega+\omega^2=0) \end{aligned}$$

$$\therefore y = x - 5$$

$$\Rightarrow x = y + 5$$

$$= -12 + 5, 6 + 5, 6 + 5$$

$$\therefore x = -7, 11, 11$$

Ans.